

1. $I_1 = \underline{0.50 \text{ A}}$ (The current is equal in the same branch)

$$I_2 = 0.50 \text{ A} - 0.20 \text{ A} = \underline{0.30 \text{ A}} \text{ (The total current splits at the junction)}$$

$$I_3 = I_2 = \underline{0.30 \text{ A}} \text{ (The current is equal in the same branch)}$$

$$I_4 = \underline{0.20 \text{ A}} \text{ (The current is equal in the same branch)}$$

$$U_3 = U_0 = \underline{6.0 \text{ V}} = U_1 + 4.5 \text{ V} \text{ (In a parallel circuit the voltage is the same across all branches)}$$

$$U_1 + 4.5 \text{ V} = 6.0 \text{ V} \Rightarrow U_1 = \underline{1.5 \text{ V}} \text{ (In a series circuit the voltage is divided among the resistors)}$$

$$R_1 = \frac{U_1}{I_2} = \frac{1.5 \text{ V}}{0.30 \text{ A}} = \underline{5.0 \Omega} \quad R_2 = \frac{U_2}{I_2} = \frac{4.5 \text{ V}}{0.30 \text{ A}} = \underline{15 \Omega} \quad R_3 = \frac{U_3}{I_4} = \frac{6.0 \text{ V}}{0.20 \text{ A}} = \underline{30 \Omega}$$

2. a) In a series circuit the current through all lamps is the same: $\underline{78 \text{ mA}}$
- b) In a series circuit the total voltage is the sum of the individual voltages. All lamps are identical and the voltage is divided equally: $U_1 = U_2 = U_3 = \frac{U_{\text{total}}}{3} = \frac{4.5 \text{ V}}{3} = \underline{1.5 \text{ V}}$
3. a) In a parallel circuit the total current is the sum of the individual currents. All lamps are identical and the current is divided equally: $I_1 = I_2 = I_3 = \frac{I_{\text{total}}}{3} = \frac{78 \text{ mA}}{3} = \underline{26 \text{ mA}}$
- b) In a parallel circuit the voltage is the same over all branches.

4. $I_1 = 0.24 \text{ A}$ (equal current in the same branch)

$$I_3 = 0.40 \text{ A} \text{ (total current is the same on both sides)}$$

$$I_2 = I_3 - I_1 = 0.4 \text{ A} - 0.24 \text{ A} = 0.16 \text{ A} \text{ (the total current splits at the junction)}$$

$$U_3 = R_3 \cdot I_3 = 12 \Omega \cdot 0.4 \text{ A} = 4.8 \text{ V}$$

$$U_1 = U_0 - U_3 = 6 \text{ V} - 4.8 \text{ V} = 1.2 \text{ V} \text{ (voltage is divided in a series circuit)}$$

$$U_2 = U_1 = 1.2 \text{ V} \text{ (in a parallel circuit the voltage is the same across all branches)}$$

$$R_1 = \frac{U_1}{I_1} = \frac{1.2 \text{ V}}{0.24 \text{ A}} = 5 \Omega$$

$$R_2 = \frac{U_2}{I_2} = \frac{1.2 \text{ V}}{0.16 \text{ A}} = 7.5 \Omega$$

$$P_1 = U_1 \cdot I_1 = 1.2 \text{ V} \cdot 0.24 \text{ A} = 0.288 \text{ W}$$

$$P_2 = U_2 \cdot I_2 = 1.2 \text{ V} \cdot 0.16 \text{ A} = 0.192 \text{ W}$$

$$P_3 = U_3 \cdot I_3 = 4.8 \text{ V} \cdot 0.4 \text{ A} = 1.92 \text{ W}$$

5. a) The voltage across the resistor is $230 \text{ V} - 12.0 \text{ V} = 218 \text{ V}$

The same amount of current passes through the lamp and the resistor (series circuit):

2.50 A

$$\text{Therefore } R = \frac{U}{I} = \frac{218 \text{ V}}{2.50 \text{ A}} = \underline{\underline{87.2 \Omega}}$$

b) $P_{\text{lamp}} = U_{\text{lamp}} \cdot I_{\text{lamp}} = 12.0 \text{ V} \cdot 2.50 \text{ A} = \underline{\underline{30.0 \text{ W}}}$

$$P_{\text{resistor}} = U_{\text{resistor}} \cdot I_{\text{resistor}} = 218 \text{ V} \cdot 2.50 \text{ A} = \underline{\underline{545 \text{ W}}}$$

The power consumed by the resistor is almost twenty times greater than the power consumed by the lamp

6. $U = R_1 \cdot I = 6.00 \Omega \cdot 0.100 \text{ A} = 0.600 \text{ V}$

0.100 A are passing through R_1 . The total current is 6.00 A , therefore the current through R_2 is

$$I_2 = I_{\text{total}} - I_1 = 6.00 \text{ A} - 0.100 \text{ A} = 5.90 \text{ A}$$

The voltage is the same in both branches of the parallel circuit:

$$R_2 = \frac{U}{I_2} = \frac{0.600 \text{ V}}{5.90 \text{ A}} = \underline{\underline{0.102 \Omega}}$$

7. **A:** Series circuit: The equivalent resistance is the sum of the individual resistances, the total voltage is the sum of the individual voltages, the current is the same through all resistors.

$$R_{\text{total}} = R_1 + R_2 + R_3 + R_4 = 10 \Omega + 20 \Omega + 50 \Omega + 100 \Omega = \underline{\underline{180 \Omega}}$$

$$\text{The current is the same through all the resistors: } I = \frac{U}{R_{\text{tot}}} = \frac{24 \text{ V}}{180 \Omega} = \underline{\underline{0.133 \text{ A}}}$$

$$\begin{aligned} \text{The individual voltages are: } U_1 &= I \cdot R_1 = \underline{\underline{1.33 \text{ V}}} & U_2 &= I \cdot R_2 = \underline{\underline{2.66 \text{ V}}} \\ U_3 &= I \cdot R_3 = \underline{\underline{6.66 \text{ V}}} & U_4 &= I \cdot R_4 = \underline{\underline{13.3 \text{ V}}} \end{aligned}$$

B: Parallel circuit: First calculate the equivalent resistance:

$$\frac{1}{R_{\text{eq}}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4}$$

$$R_{\text{eq}} = \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4} \right)^{-1} = \left(\frac{1}{10 \Omega} + \frac{1}{20 \Omega} + \frac{1}{50 \Omega} + \frac{1}{100 \Omega} \right)^{-1} = \underline{\underline{5.55 \Omega}}$$

The voltage is the same in all the branches: $U_1 = U_2 = U_3 = U_4 = \underline{\underline{24 \text{ V}}}$.

$$\begin{aligned} \text{The individual currents are } I_1 &= \frac{U}{R_1} = \frac{24 \text{ V}}{10 \Omega} = \underline{\underline{2.4 \text{ A}}}, & I_2 &= \frac{U}{R_2} = \frac{24 \text{ V}}{20 \Omega} = \underline{\underline{1.2 \text{ A}}}, \\ I_3 &= \frac{U}{R_3} = \frac{24 \text{ V}}{50 \Omega} = \underline{\underline{0.48 \text{ A}}}, & I_4 &= \frac{U}{R_4} = \frac{24 \text{ V}}{100 \Omega} = \underline{\underline{0.24 \text{ A}}} \end{aligned}$$

C: Combination of series and parallel circuits. First calculate the equivalent resistances of R_1 and R_2 , and of R_3 and R_4 :

$$R_{\text{eq}(1,2)} = R_1 + R_2 = 10 \, \Omega + 20 \, \Omega = 30 \, \Omega$$

$$R_{\text{eq}(3,4)} = R_3 + R_4 = 50 \, \Omega + 100 \, \Omega = 150 \, \Omega$$

$R_{\text{eq}(1,2)}$ and $R_{\text{eq}(3,4)}$ are connected in parallel, therefore:

$$R_{\text{eq}(1,2,3,4)} = \frac{R_{\text{eq}(1,2)} \cdot R_{\text{eq}(3,4)}}{R_{\text{eq}(1,2)} + R_{\text{eq}(3,4)}} = \frac{30 \, \Omega \cdot 150 \, \Omega}{30 \, \Omega + 150 \, \Omega} = \underline{\underline{25 \, \Omega}}$$

$$\text{The current in the upper branch is } I_{12} = \frac{U}{R_{12}} = \frac{24 \, \text{V}}{30 \, \Omega} = \underline{\underline{0.8 \, \text{A}}}$$

$$\text{The current in the lower branch is } I_{34} = \frac{U}{R_{34}} = \frac{24 \, \text{V}}{150 \, \Omega} = \underline{\underline{0.16 \, \text{A}}}$$

The voltage is the same in each of the branches of the parallel circuit. The individual voltages are

$$U_1 = I \cdot R_{12} = \underline{\underline{8 \, \text{V}}} \qquad U_2 = I \cdot R_{12} = \underline{\underline{16 \, \text{V}}}$$

$$U_3 = I \cdot R_{34} = \underline{\underline{8 \, \text{V}}} \qquad U_4 = I \cdot R_{34} = \underline{\underline{16 \, \text{V}}}$$

D: Combination of series and parallel circuits. First calculate the equivalent resistance of R_2 , R_3 and R_4 :

$$R_{\text{eq}(2,3,4)} = \left(\frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4} \right)^{-1} = \left(\frac{1}{20 \, \Omega} + \frac{1}{50 \, \Omega} + \frac{1}{100 \, \Omega} \right)^{-1} = 12.5 \, \Omega$$

R_1 and $R_{\text{eq}(2,3,4)}$ are in parallel, thus:

$$R_{\text{eq}(1,2,3,4)} = R_1 + R_{\text{eq}(2,3,4)} = 10 \, \Omega + 12.5 \, \Omega = \underline{\underline{22.5 \, \Omega}}$$

$$\text{The total current passes through } I_1, \text{ thus } I_1 = I_{\text{total}} = \frac{U_{\text{total}}}{R_{\text{eq}(1,2,3,4)}} = \frac{24 \, \text{V}}{22.5 \, \Omega} = \underline{\underline{1.07 \, \text{A}}}$$

The total current passes through R_1 , thus the voltage across R_1 is

$$U_1 = R_1 \cdot I_{\text{total}} = 10 \, \Omega \cdot 1.07 \, \text{A} = \underline{\underline{10.7 \, \text{V}}}$$

The remaining voltage is applied across the three branches of the parallel circuit, therefore

$$U_2 = U_3 = U_4 = U_{\text{total}} - U_1 = 24.0 \, \text{V} - 10.7 \, \text{V} = \underline{\underline{13.3 \, \text{V}}}$$

The individual currents through the resistors R_2 , R_3 and R_4 are:

$$I_2 = \frac{U_2}{R_2} = \frac{13.3 \, \text{V}}{20 \, \Omega} = \underline{\underline{0.66 \, \text{A}}} \qquad I_3 = \frac{U_3}{R_3} = \frac{13.3 \, \text{V}}{50 \, \Omega} = \underline{\underline{0.27 \, \text{A}}}$$

$$I_4 = \frac{U_4}{R_4} = \frac{13.3 \, \text{V}}{100 \, \Omega} = \underline{\underline{0.13 \, \text{A}}}$$

$$8. \text{ a) } R (60\text{W-light bulb}) = \frac{U^2}{P} = \frac{(220 \text{ V})^2}{60 \text{ W}} = \underline{\underline{807 \, \Omega}}$$

$$R (100\text{W-light bulb}) = \frac{U^2}{P} = \frac{(220 \text{ V})^2}{100 \text{ W}} = \underline{\underline{484 \, \Omega}}$$

$$R_{\text{total}} = R_{60\text{W}} + R_{100\text{W}} = 807 \, \Omega + 484 \, \Omega = \underline{\underline{1291 \, \Omega}}$$

$$\text{b) } I = \frac{U}{R} = \frac{220 \text{ V}}{1291 \, \Omega} = \underline{\underline{0.17 \text{ A}}}$$

$$\text{c) } U (60 \text{ W-light bulb}) = R_{60\text{W}} \cdot I = 807 \, \Omega \cdot 0.17 \text{ A} = \underline{\underline{138 \text{ V}}}$$

$$U (100 \text{ W-light bulb}) = R_{100\text{W}} \cdot I = 484 \, \Omega \cdot 0.17 \text{ A} = \underline{\underline{82 \text{ V}}}$$

$$\text{d) } P (60 \text{ W-light bulb}) = U_{60\text{W}} \cdot I = 138 \text{ V} \cdot 0.17 \text{ A} = \underline{\underline{23.5 \text{ W}}}$$

$$P (100 \text{ W-light bulb}) = U_{100\text{W}} \cdot I = 82 \text{ V} \cdot 0.17 \text{ A} = \underline{\underline{13.9 \text{ W}}}$$